

## Components of Flow Processes

Equipment used to extract/provide work and/or heat from a process

- turbines - generate electricity
- compressors and pumps - move fluid, change pressures
- heat exchangers - change temperature of fluid
- throttles - change pressure

### OBJECTIVES

- evaluate performance of components of flow processes through appropriate mass, energy, entropy balances

## Table 7.1 Pg 256 of SvNA

Table 7.1: Equations of Balance

General Equations of Balance	Balance Equations for Steady-Flow Processes	Balance Equations for Single-Stream Steady-Flow Processes
$\frac{dm_{cv}}{dt} + \Delta(\dot{m})_{fs} = 0 \quad (2.25)$	$\Delta(\dot{m})_{fs} = 0 \quad (7.1)$	$\dot{m}_1 = \dot{m}_2 = \dot{m} \quad (7.2)$
$\frac{d(mU)_{cv}}{dt} + \Delta \left[ \left( H + \frac{1}{2}u^2 + zg \right) \dot{m} \right]_{fs} = \dot{Q} + \dot{W} \quad (2.28)$	$\Delta \left[ \left( H + \frac{1}{2}u^2 + zg \right) \dot{m} \right]_{fs} = \dot{Q} + \dot{W}_s \quad (2.30)$	$\Delta H + \frac{\Delta u^2}{2} + g\Delta z = Q + W_s \quad (2.32a)$
$\frac{d(mS)_{cv}}{dt} + \Delta(S\dot{m})_{fs} - \sum_j \frac{\dot{Q}_j}{T_{\sigma,j}} = \dot{S}_G \geq 0 \quad (5.21)$	$\Delta(S\dot{m})_{fs} - \sum_j \frac{\dot{Q}_j}{T_{\sigma,j}} = \dot{S}_G \geq 0 \quad (5.22)$	$\Delta S - \sum_j \frac{Q_j}{T_{\sigma,j}} = S_G \geq 0 \quad (5.23)$

# Turbines

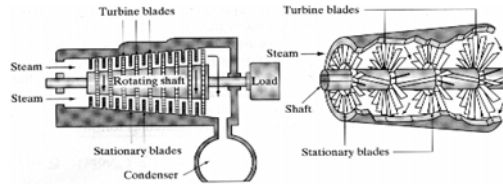
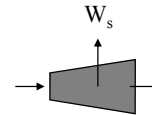


Figure 3.3-3 Sketch of a steam turbine. (Adapted from *The World Book Encyclopedia*, Field Educational Enterprises, New York, 1976.)



1 MW turboexpander

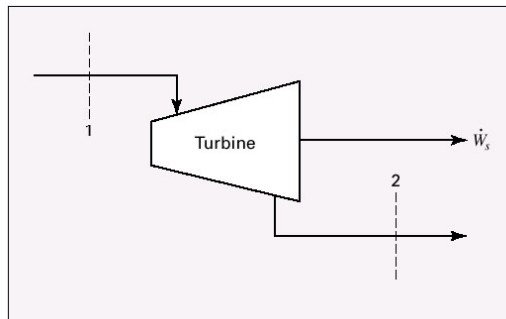
convert gas kinetic energy into work,  $W_s$

$$\Delta H = T_\sigma (\Delta S_{fs} - S_{gen}) + W_s$$

$$\eta_{\text{turbine}} = \frac{W_s}{(W_s)_S} = \frac{\Delta H}{(\Delta H)_S}$$

efficiency

## Figure 7.3: Schematic of Turbine



At steady state an ideal (reversible) turbine converts all the enthalpy change between point 1 and 2 entirely into shaft work.

$$(\Delta H)_S = (W_s)_S$$

Note irritating nomenclature  $s$   
 $\rightarrow$  shaft  
 $S \rightarrow$  isentropic ( $\Delta S=0$ )

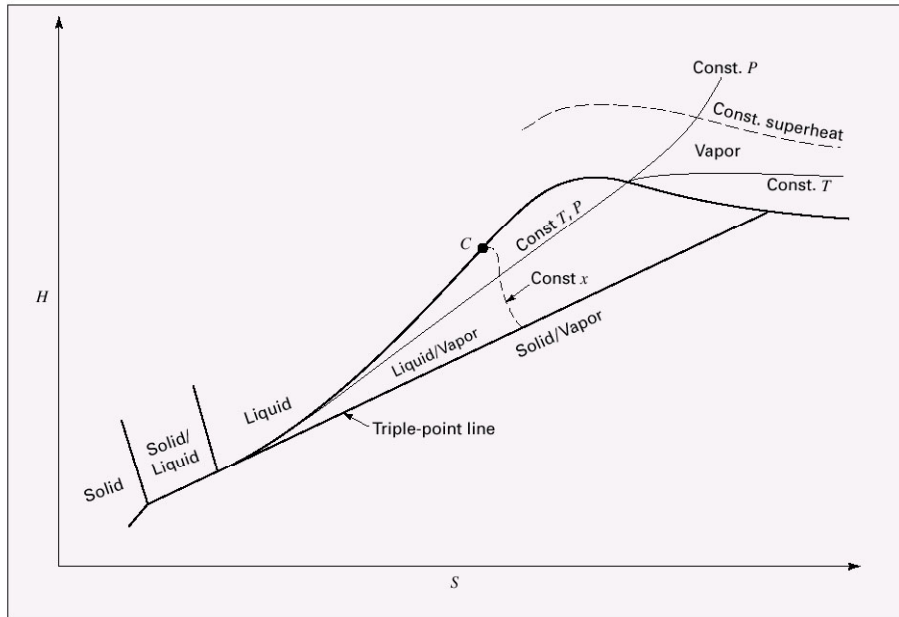


Figure 6.4: Mollier diagram.

## Mollier Diagram – Seriously Complicated

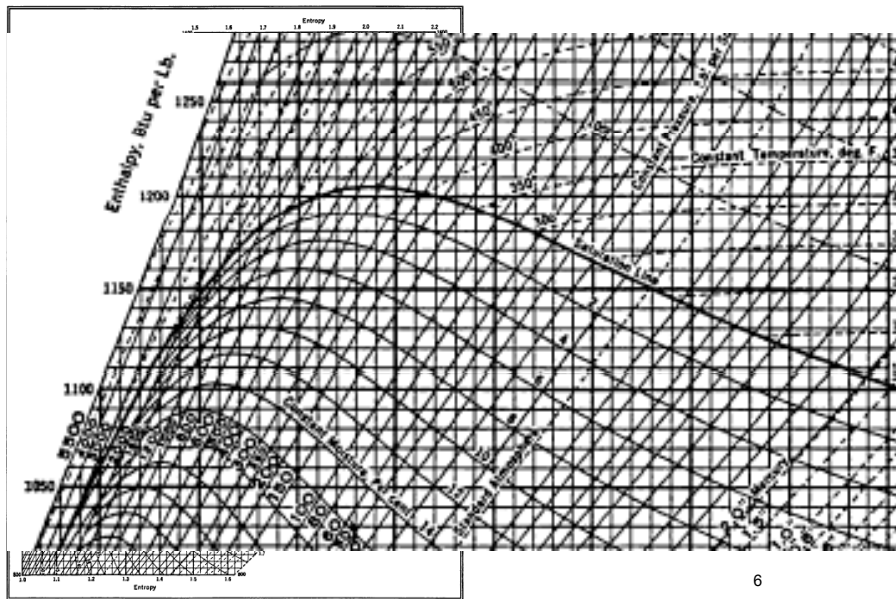
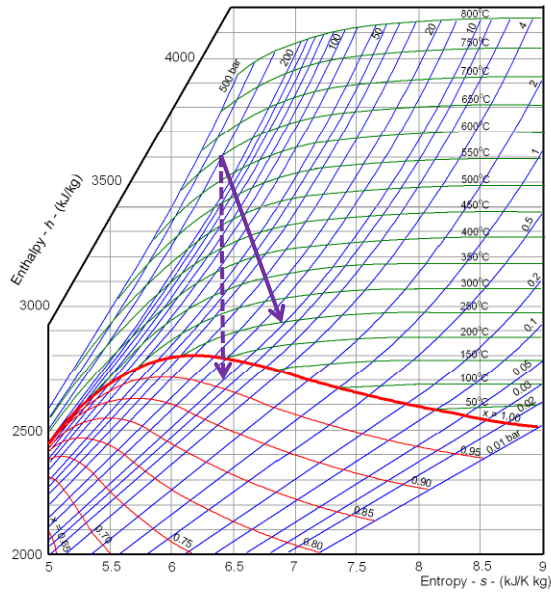


Figure A-1

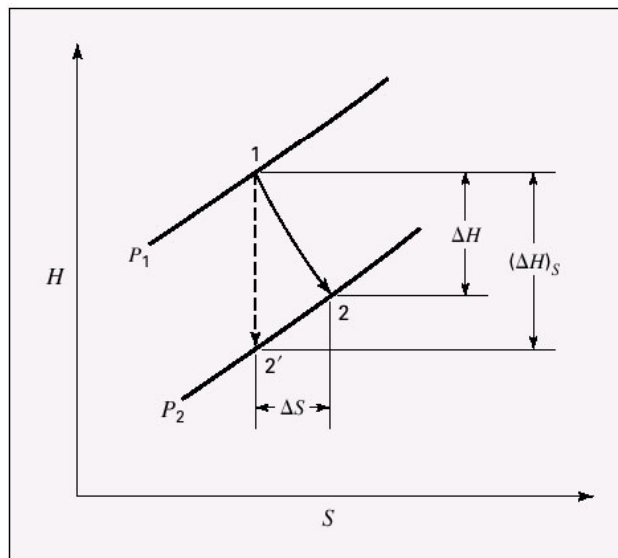
## Mollier Diagram (a bit less confusing)



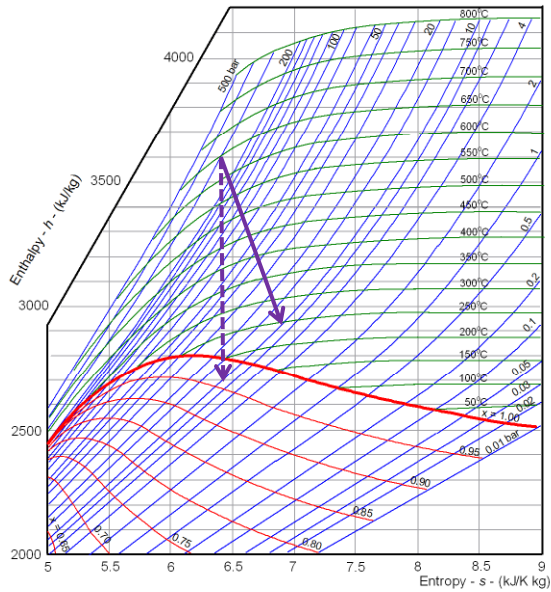
- Key points
- Vertical lines are constant entropy (remember that when  $\Delta S=0$  we have reversible process  $\rightarrow$  most work possible)
  - Turbines turn enthalpy into work

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Figure 7.4: Efficiency from Mollier Diagram



## Mollier Diagram – Turbine Efficiency



$$\eta_{\text{turbine}} = \frac{W_s}{(W_s)_s} = \frac{\Delta H}{(\Delta H)_s}$$

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## Turbine – Efficiency from Steam Tables

A turbine is fed with steam at 475°C and 100 bar. The steam leaves the turbine saturated at 10 bar. The quality of the exiting steam is 1.0. Calculate the adiabatic efficiency of the turbine using steam tables.

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Table F.2. Superheated Steam, SI Units (Continued)

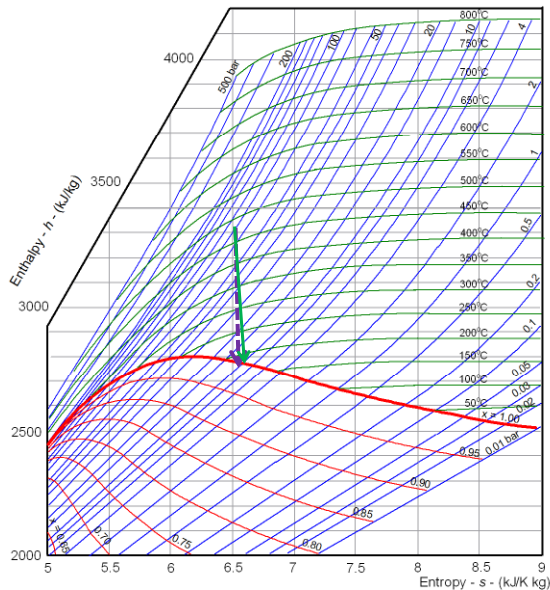
Pg 730-1 of SVA

P/kPa (t <sup>sat</sup> /°C)	sat. liq.	sat. vap.	TEMPERATURE: t °C (TEMPERATURE: T kelvins)								
			175 (448.15)	200 (473.15)	220 (493.15)	240 (513.15)	260 (533.15)	280 (553.15)	300 (573.15)	325 (598.15)	
750 (167.76)	V	1.112	255.43	260.88	279.05	293.03	306.65	320.01	333.17	346.19	362.32
	U	708.467	2573.3	2586.9	2632.1	2666.8	2700.6	2733.7	2766.4	2798.9	2839.3
	H	709.301	2764.8	2782.5	2841.4	2886.6	2930.6	2973.7	3016.3	3058.5	3111.0
775 (169.10)	S	2.0195	6.6817	6.7215	6.8494	6.9429	7.0303	7.1128	7.1912	7.2662	7.3558
	V	1.113	247.61	251.93	269.63	283.22	296.45	309.41	322.19	334.81	350.44
	U	714.326	2574.3	2585.4	2631.0	2665.9	2699.8	2733.1	2765.9	2798.4	2838.9
800 (170.41)	H	715.189	2766.2	2780.7	2840.0	2885.4	2929.6	2972.9	3015.6	3057.9	3110.5
	S	2.0328	6.6705	6.7031	6.8319	6.9259	7.0137	7.0965	7.1751	7.2502	7.3400
	V	1.115	240.26	243.53	260.79	274.02	286.88	299.48	311.89	324.14	339.31
1000 (179.88)	U	720.043	2575.3	2584.0	2629.9	2665.0	2699.1	2732.5	2765.4	2797.9	2838.5
	H	720.935	2767.5	2778.8	2838.6	2884.2	2928.6	2972.1	3014.9	3057.3	3109.9
	V	1.127	194.29	.....	205.92	216.93	227.55	237.89	248.01	257.98	270.27
1050 (182.02)	U	761.478	2581.9	.....	2620.9	2657.7	2693.0	2727.4	2761.0	2794.2	2835.2
	H	762.605	2776.2	.....	2826.8	2874.6	2920.6	2965.2	3009.0	3052.1	3105.5
	S	2.1382	6.5828	.....	6.6922	6.7911	6.8825	6.9680	7.0485	7.1251	7.2163
1100 (184.07)	V	1.130	185.45	.....	195.45	206.04	216.24	226.15	235.84	245.37	257.12
	U	770.843	2583.3	.....	2618.5	2655.8	2691.5	2726.1	2759.9	2793.2	2834.4
	H	772.029	2778.0	.....	2823.8	2872.1	2918.5	2963.5	3007.5	3050.8	3104.4
1150 (186.05)	S	2.1588	6.5659	.....	6.6645	6.7647	6.8569	6.9430	7.0240	7.1009	7.1924
	V	1.133	177.38	.....	185.92	196.14	205.96	215.47	224.77	233.91	245.16
	U	779.878	2584.5	.....	2616.2	2653.9	2689.9	2724.7	2758.8	2792.2	2833.6
1150 (186.05)	H	781.124	2779.7	.....	2820.7	2869.6	2916.4	2961.8	3006.0	3049.6	3103.3
	S	2.1786	6.5497	.....	6.6379	6.7392	6.8323	6.9190	7.0005	7.0778	7.1695
	V	1.136	169.99	.....	177.22	187.10	196.56	205.73	214.67	223.44	234.25
1150 (186.05)	U	788.611	2585.8	.....	2613.8	2651.9	2688.3	2723.4	2757.7	2791.3	2832.8
	H	789.917	2781.3	.....	2817.6	2867.1	2914.4	2960.0	3004.5	3048.2	3102.2
	S	2.1977	6.5342	.....	6.6122	6.7147	6.8086	6.8959	6.9779	7.0556	7.1476
1150 (186.05)	V	1.139	163.20	.....	169.23	178.80	187.95	196.79	205.40	213.85	224.24

Table F.2. Superheated Steam, SI Units (Continued)

P/kPa (t <sup>sat</sup> /°C)		sat. liq.	sat. vap.	TEMPERATURE: t °C (TEMPERATURE: T kelvins)							
				475 (748.15)	500 (773.15)	525 (798.15)	550 (823.15)	575 (848.15)	600 (873.15)	625 (898.15)	650 (923.15)
8200 (296.70)	V	1.391	22.863	38.893	40.614	42.295	43.943	45.566	47.166	48.747	50.313
	U	1315.2	2569.5	3015.6	3063.3	3110.5	3157.4	3204.3	3251.1	3298.1	3345.2
	H	1326.6	2757.0	3334.5	3396.4	3457.3	3517.8	3577.9	3637.9	3697.8	3757.7
8400 (298.39)	S	3.2239	5.7338	6.6311	6.7124	6.7900	6.8646	6.9365	7.0062	7.0739	7.1397
	V	1.398	22.231	37.887	39.576	41.224	42.839	44.429	45.996	47.544	49.076
	U	1324.3	2567.2	3013.6	3061.6	3109.9	3155.9	3202.9	3249.8	3296.9	3344.1
10000 (310.96)	H	1336.1	2754.0	3331.9	3394.0	3455.2	3515.8	3576.1	3636.2	3696.2	3756.3
	S	3.2399	5.7207	6.6173	6.6990	6.7769	6.8516	6.9238	6.9936	7.0614	7.1274
	V	1.404	21.627	36.928	38.586	40.202	41.787	43.345	44.880	46.397	47.897
10200 (312.42)	U	1322.2	2564.0	3011.6	3059.9	3107.9	3154.4	3201.5	3248.5	3295.7	3342.9
	S	3.2605	5.6198	6.5147	6.5994	6.6797	6.7564	6.8302	6.9013	6.9703	7.0373
	V	1.460	17.605	30.599	32.058	33.472	34.851	36.202	37.530	38.837	40.128
10400 (313.86)	U	1401.8	2544.6	2995.3	3045.2	3094.0	3142.3	3190.3	3238.2	3286.1	3334.0
	H	1416.7	2724.2	3307.4	3372.1	3435.5	3497.8	3559.6	3621.0	3682.2	3743.3
	S	3.3748	5.6076	6.5027	6.5879	6.6685	6.7454	6.8194	6.8907	6.9598	7.0269
10600 (315.27)	V	1.467	17.184	29.943	31.382	32.776	34.134	35.464	36.770	38.056	39.325
	U	1410.0	2541.8	2993.2	3043.3	3092.4	3140.8	3188.9	3236.9	3284.8	3332.9
	H	1425.2	2720.6	3304.6	3369.7	3433.2	3495.8	3557.8	3619.3	3680.6	3741.8
10800 (316.68)	S	3.3889	5.5955	6.4909	6.5765	6.6574	6.7346	6.8087	6.8803	6.9495	7.0167
	V	1.474	16.778	29.313	30.732	32.106	33.444	34.753	36.039	37.304	38.552
	U	1418.1	2539.0	2991.1	3041.4	3090.7	3139.3	3187.5	3235.6	3283.6	3331.7
11000 (318.09)	H	1433.7	2716.9	3301.8	3367.2	3431.0	3493.8	3555.9	3617.6	3679.1	3740.4
	S	3.4029	5.5835	6.4793	6.5652	6.6465	6.7239	6.7983	6.8700	6.9394	7.0067
	V	1.481	16.372	28.688	30.087	31.441	32.750	34.024	35.273	36.507	37.726

### Mollier Diagram – Turbine Efficiency

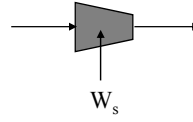
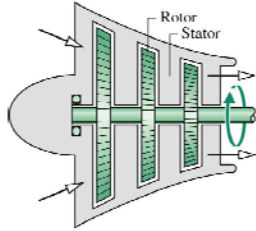


$$\eta_{\text{turbine}} = \frac{W_s}{(W_s)_S} = \frac{\Delta H}{(\Delta H)_S}$$

The Mollier diagram is much quicker if perhaps not as accurate.

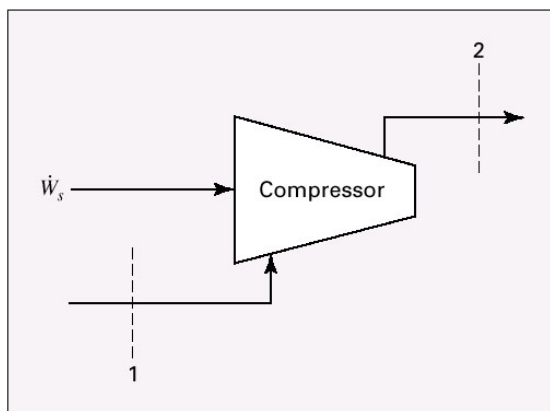
## Compressors

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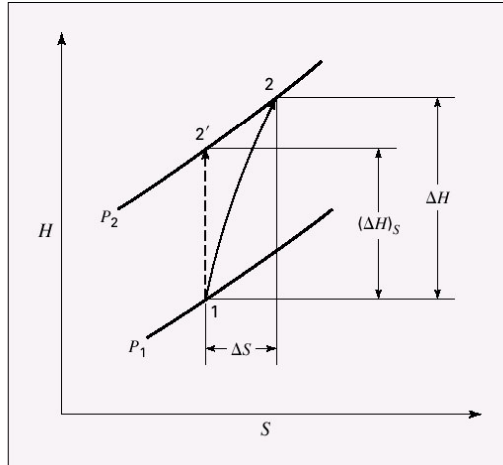


used to transport **gases**

$$\eta_{\text{comp}} = \frac{(W_s)_S}{W_s} = \frac{(\Delta H)_S}{\Delta H}$$

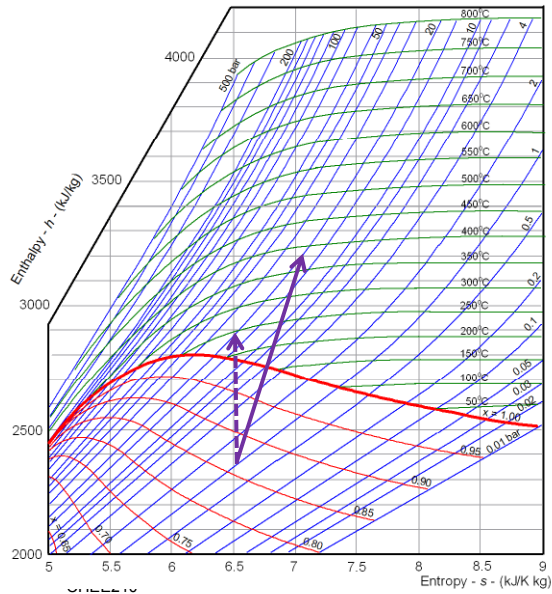


## Compressor on the Mollier Diagram



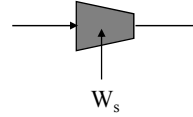
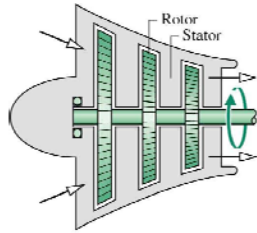
- On the Mollier diagram the change in enthalpy  $(\Delta H)_{\Delta S=0} < (\Delta H)_{\Delta S>0}$

## Mollier Diagram for Compression



-Vertical lines are constant entropy ( $\Delta S=0$  means we have a reversible compressor that requires the least work for compression)  
 - In a real compressor  $\Delta S>0$  and more work is required.  
 - On the Mollier diagram the change in enthalpy  $(\Delta H)_{\Delta S=0} < (\Delta H)_{\Delta S>0}$

## Compressors

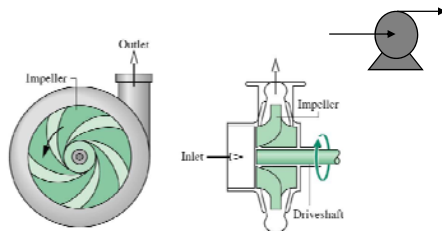


$$\eta_{\text{comp}} = \frac{(W_s)_S}{W_s} = \frac{(\Delta H)_S}{\Delta H}$$

From the Mollier diagram for compression of steam from 1 bar 100°C, quality 0.867 to 20 bar and superheated to 375°C. Reading directly off Mollier Diagram

$$\eta_{\text{comp}} = \frac{(W_s)_S}{W_s} = \frac{(\Delta H)_S}{\Delta H} = \frac{(2880 - 2360)_S}{(3200 - 2360)} = \frac{(520)_S}{840} = 0.62$$

## Pumps



used to transport **liquids**

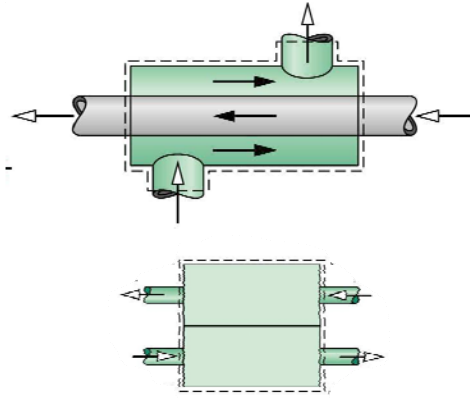
$$\eta_{\text{pump}} = \frac{(W_s)_S}{W_s} = \frac{(\Delta H)_S}{\Delta H}$$

$$(\Delta H)_S = V(P_e - P_i)$$

## Heat Exchanger

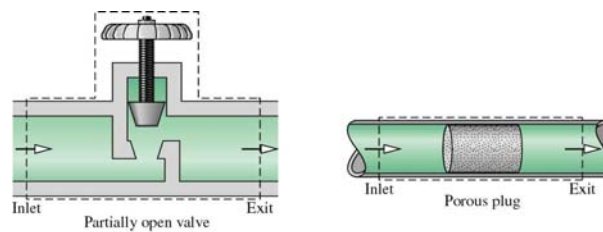
Fluid flow through a system of pipes with transfer of heat energy from one fluid to another.

$$\sum \dot{m}_i H_i = \sum \dot{m}_e H_e$$



## Throttle

Fluid flowing in a pipe suddenly encounters a restriction. Result is a pressure drop at constant enthalpy.



## Example

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A compressor takes in gas at a lower pressure and discharges it at a higher temperature. The process occurs quickly, therefore it can safely be assumed to be adiabatic. Air (ideal gas,  $C_p = 29.3$  J/(mol K)) is the inlet gas at  $T = 290$  K and  $P = 1$  atm. The outlet pressure is 10 atm. Estimate the  $T$  of the gas and the rate at which work is done on the gas for a flow rate of 2.5 mol/s.